# Crystal Structure of $\mathrm{Ba}_{6} \mathbf{Z n} \mathbf{n}_{\mathbf{7}} \mathbf{F}_{\mathbf{2 6}}$ 

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#### Abstract

$\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ is monoclinic (S.G. C2/m): $a=19.46(1) \AA, b=5.956(2) \AA, c=12.243(5) \AA, \beta=128.88(1)^{\circ}$, $Z=2$. The structure has been refined from 1730 independent reflections to $R=0.046$ ( $R_{\omega}=0.049$ ). The three dimensional network can be described as layers containing intergrown rutile and perovskite units. Two layers are connected by isolated octahedra. An alternative description uses defective rutile blocks joined by isolated octahedra. The comparison with the $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ structure suggests a "condensation" mechanism which could explain the progressive transformation from perovskite related structures to the rutile structure. All the $\mathrm{Ba}^{2+}$ (three (4i) sites), form a dense packing with $\mathrm{F}^{-}$. They are dodeca-coordinated, with the hcp and fcc type for $\mathrm{Ba}_{3}$ and ( $\mathrm{Ba}_{1} / \mathrm{Ba}_{2}$ ), respectively. © 1985 Academic Press. Inc.


## Introduction

In the binary systems $\mathrm{BaF}_{2}-M \mathrm{~F}_{2}$ ( $M=$ $\mathrm{Co}, \mathrm{Ni}, \mathrm{Cu}, \mathrm{Zn}(1)$ ), many compounds appear for a molar ratio $M / \mathrm{Ba}>1$. Starting from the composition $\mathrm{BaMF} \mathrm{F}_{4}$ whose bidimensional structure is well known ( 2,3 ), the increase of the $M / \mathrm{Ba}$ ratio successively leads to $\mathrm{Ba}_{6} M_{7} \mathrm{~F}_{26}(M=\mathrm{Cu}, \mathrm{Zn}), \mathrm{Ba}_{2} M_{3} \mathrm{~F}_{10}$ ( $M=\mathrm{Zn}$ (4), $\mathrm{Co}, \mathrm{Ni}$ ), and $\mathrm{Ba}_{2} M_{7} \mathrm{~F}_{18}(M=$ $\mathrm{Ni}, \mathrm{Cu}, \mathrm{Zn}$ ). After the structural determination of $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ that we performed some years ago (5), we are now investigating the crystal structure of the other compounds. This paper is devoted to $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$, which was previously formulated $\mathrm{Ba}_{5} \mathrm{Zn}_{6} \mathrm{~F}_{22}$ (I). Its structure will be compared with $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ in order to show the progressive intergrowth of perovskite and rutile blocks when $M / \mathrm{Ba}$ increases.

## Experimental

Transparent platelets of $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ are grown either by hydrothermal synthesis in $49 \% \mathrm{HF}\left[\mathrm{BaF}_{2}\right]=6 \mathrm{M},\left[\mathrm{MF}_{2}\right]=7 \mathrm{M}$ at $400^{\circ} \mathrm{C}, 205 \mathrm{MPa}$ for 3 days according to a method previously described ( 6 ) or by long heating ( $750^{\circ} \mathrm{C}-2$ weeks) of a stoichiometric mixture of the corresponding fluorides in sealed platinum tubes. (100) planes correspond to the largest dimensions of the platelets (Table I).

Despite an orthorhombic pseudosymmetry, Laue and precession photographs show that the true symmetry of the crystals is monoclinic, with space group $C 2 / m$ (Table I). Intensity data were coliected on a CAD 4 Nonius diffractometer. The experimental conditions of data collection are summarized in Table II. Corrections for

Lorentz, polarization effects and for absorption are applied, using the SHELX program (7) for all calculations. Atomic scattering factors are taken from the "International Tables for X-Ray Crystallography" (8) for $\mathrm{Ba}^{2+}, \mathrm{Zn}^{2+}, \mathrm{F}^{-}$.

## Structure Determination

The structure has been solved from a Patterson map which allows us to localize the 12 barium ions of the cell in three $4 i$ sites $x 0 z$. The refinement of the corresponding coordinates leads to a reliability factor of 0.421 . A Fourier map then reveals the position of the $\mathrm{Zn}^{2+}$ ions ( $R=0.135$ ). The $\mathrm{F}^{-}$ ions are located from a new Fourier synthesis. The refinement of their atomic parameters and isotropic temperature factors easily converges to $R=0.064$ ( $R_{\omega}=0.064$ ). The residual falls to 0.046 ( $R_{t, s}=0.049$ ) when applying anisotropic thermal motion for all atoms and a secondary extinction factor of $5.1 \times 10^{-8}$. A final difference Fourier map gives a maximum peak of 2.3 $e^{-/} / \AA^{3}$ corresponding to a position close to Ba 2 ion. Refinements in the noncentric $C 2$ and Cm space groups do not improve the results.

Table III presents the final results for the 16 independent positions; characteristic distances are listed in Tables IV and VII. The list of structure factors can be obtained on request to one of the authors (G.F.).

## Discussion of the Structure

Figure 1 presents the ( 010 ) projection of

TABLE I
Experimental Data for $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ Crystals

| Symmetry: monoclinic | Cell paramelers | $a=19.46(1) \AA$ |
| :--- | :--- | :--- |
| Space group: $C 2 / m$ (no 12) |  | $b=5.956(2) \AA$ |
| Conditions: $h+k=2 n$ | $c=12.243(5) \AA$ |  |
| $\rho_{\text {exp }}: 5.23(11) \mathrm{g} \cdot \mathrm{cm}^{-3}$ | $\beta=128.88(1)^{\circ}$ |  |
| $\rho_{\text {calc }} 5.32 \mathrm{~g} \cdot \mathrm{~cm}^{-3}$ |  | $V=1104 \AA^{3}$ |
|  | $Z=2$ |  |

TABLE II
Characteristics of Data Collection
Crystal dimensions: $0.07 \times 0.07 \times 0.025 \mathrm{~mm}^{3}$ Radiation: MoKa
Linear absorption coefficient: $184 \mathrm{~cm}^{-1}$
$\left.\begin{array}{rlrl}\text { Range measured: } & 2^{\circ} & <\theta<35^{\circ} & -26\end{array}\right)$
Reflections measured:

| Total | 3447 | $R=0.046$ |
| :--- | :--- | ---: |
| Independent | 1983 | $R_{\omega}=0.049$ |

With $|F| / \sigma(|F|)>6 \quad 1730$
Secondary extinction: $5.1(4) \times 10^{-8}$
Transmission factor maximum: 0.648 ; minimum: 0.310

Operating features:
Monochromator: graphite
Scan mode: $\omega-2 \theta \quad$ sweep $S=(1.80+0.45 \operatorname{tg} 2 \theta)^{\circ}$
Scintillation counter aperture: 3.00 mm
Scanning speed: $v=(20.1166 / \mathrm{NV})^{\circ} \cdot \mathrm{mn}^{-1}$ with NV integer
$\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$. Zinc ions occupy four kinds of crystallographic sites, and are all roughly hexacoordinated by $\mathrm{F}^{-}$(Table IV). All the fluorine atoms of $\mathrm{Zn}(1)$ and $\mathrm{Zn}(4)$ octahedra are bridging ones. $\mathrm{Zn}(2)$ octahedra possess four terminal and two bridging $\mathrm{F}^{-}$. The inverse situation occurs with $\mathrm{Zn}(3)$. It is noteworthy that there are two kinds of bridging fluorine ions in the structure: they can belong to two or three octahedra (Table V)


Fig. 1. (010) projection of $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$. Shaded octahedra correspond to the rutile chains which develop along [010]. The numbers refer to the type of fluorine atoms of Table III. Open symbols correspond to $y=0$ and full symbols to $y=\frac{1}{2}$.

TABLE III
Atomic Coordinates and Anisotropic Thermal Parameters of $\mathrm{Ba}_{6} \mathbf{Z n}_{7} \mathrm{~F}_{26}{ }^{\text {a.b }}$

| Atom | Site | $x$ | $y$ | $z$ | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{23}$ | $U_{13}$ | $U_{12}$ | $B_{\text {eq }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ba1 | $4 i$ | $1475(1)$ | 0 | $1522(1)$ | $135(4)$ | $94(3)$ | $113(3)$ | 0 | $84(3)$ | 0 | 0,90 |
| Ba2 | $4 i$ | $1433(1)$ | $\frac{1}{2}$ | $4043(1)$ | $127(4)$ | $166(4)$ | $115(3)$ | 0 | $84(3)$ | 0 | 1,07 |
| Ba 3 | $4 i$ | $3437(1)$ | 0 | $1054(1)$ | $127(4)$ | $115(3)$ | $137(3)$ | 0 | $86(3)$ | 0 | 1,00 |
| Zn 1 | $2 b$ | 0 | $\frac{1}{2}$ | 0 | $86(10)$ | $55(8)$ | $69(8)$ | 0 | $44(8)$ | 0 | 0,55 |
| Zn 2 | $4 i$ | $2786(1)$ | $\frac{1}{2}$ | $2879(2)$ | $102(7)$ | $76(6)$ | $118(6)$ | 0 | $75(6)$ | 0 | 0,78 |
| Zn3 | $4 i$ | $4877(1)$ | $\frac{1}{2}$ | $2215(2)$ | $140(8)$ | $98(6)$ | $112(6)$ | 0 | $87(7)$ | 0 | 0,92 |
| Zn4 | $4 h$ | $\frac{1}{2}$ | $2445(3)$ | $\frac{1}{2}$ | $142(7)$ | $70(6)$ | $99(6)$ | 0 | $76(6)$ | 0 | 0,82 |
| F1 | $8 j$ | $2586(4)$ | $2640(10)$ | $3809(6)$ | $183(28)$ | $104(24)$ | $152(25)$ | $27(20)$ | $113(24)$ | $-12(22)$ | 1,15 |
| F2 | $8 j$ | $2546(4)$ | $2697(10)$ | $1486(6)$ | $171(31)$ | $113(25)$ | $175(28)$ | $-28(20)$ | $113(27)$ | $-6(21)$ | 1,21 |
| F3 | $8 j$ | $4910(5)$ | $2349(10)$ | $3254(6)$ | $246(33)$ | $112(25)$ | $147(26)$ | $5(20)$ | $123(27)$ | $-10(24)$ | 1,33 |
| F4 | $8 j$ | $4818(7)$ | $2489(16)$ | $0923(8)$ | $564(67)$ | $569(62)$ | $181(35)$ | $-78(35)$ | $106(42)$ | $348(52)$ | 3,46 |
| F5 | $4 i$ | $4102(6)$ | 0 | $4200(10)$ | $103(39)$ | $86(34)$ | $236(43)$ | 0 | $87(37)$ | 0 | 1,12 |
| F6 | $4 i$ | $6153(8)$ | $\frac{1}{2}$ | $3278(12)$ | $173(52)$ | $701(87)$ | $240(51)$ | 0 | $144(47)$ | 0 | 2,93 |
| F7 | $4 i$ | $3599(7)$ | $\frac{1}{2}$ | $0809(10)$ | $115(44)$ | $446(61)$ | $167(41)$ | 0 | $86(38)$ | 0 | 1,92 |
| F8 | $4 i$ | $4128(6)$ | $\frac{1}{2}$ | $4204(9)$ | $129(42)$ | $85(35)$ | $199(41)$ | 0 | $73(37)$ | 0 | 1,09 |
| F9 | $4 i$ | $1290(7)$ | $\frac{1}{2}$ | $1563(11)$ | $114(47)$ | $372(61)$ | $247(51)$ | 0 | $10(42)$ | 0 | 1,93 |

${ }^{a}$ All the values are $\times 10^{4}$. Standard deviations are in parentheses.
${ }^{b}$ The vibrational coefficients are relative to the expression $T=\exp \left[-2 \pi^{2}\left(h^{2} a^{* 2} U_{11}+k^{2} b^{* 2} U_{22}+1^{2} c^{* 2} U_{33}+\right.\right.$ $\left.\left.2 k l b^{*} c^{*} U_{23}+2 h l a^{*} c^{*} U_{13}+2 h k a^{*} b^{*} U_{12}\right)\right]$.

TABLE IV
Interatomic Distances ( A ) and Bond Angles $\left({ }^{\circ}\right)$ of Zn Octahedra in $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$

| Znl Octahedron: Symmetry $2 / \mathrm{m}$ |  |  |
| :---: | :---: | :---: |
|  |  | Angle F-Zn-F |
| Zn1-F4i: $4 \times 2.025(10)$ | F4-F4: $2 \times 2.766$ | 86.14 ) |
| Zn1-F9\%: $2 \times 1.983(11)$ | F4-F9: $4 \times 2.801$ | 88.6(3) |
|  | F4-F9: $4 \times 2.872$ | 91.5(3) |
| ( Zn -F) 2.011 | F4-F4: $2 \times 2.978$ | 94.6(4) |
| Zn2 octahedron: Symmetry $m$ |  |  |
| Zn2-F1': $2 \times 1.9946$ ) | F1-F9: $2 \times 2.686$ | 77.5 (3) |
| Zn2-F2t: $2 \times 2.001(6)$ | F2-F2: 2.743 | 86.4(3) |
| Zn2-F8 ${ }^{\text {b }}$ : 2.031 (10) | F1-F2: $2 \times 2.795$ | 88.8(3) |
| Zn2-F9 ${ }^{\text {P }}$ 2.276(11) | F1-F1: $\quad 2.810$ | 89.7(3) |
|  | F2-F9: $2 \times 2.856$ | 83.4(3) |
| (Zn2-F) 2.049 | F1-F8: $2 \times 3.064$ | $99.2(3)$ |
| F8-Zn2-F9: 175.1(4) | F2-F8: $2 \times 3.089$ | 100.0(3) |
| Zn 3 octahedron: Symmetry m |  |  |
| Zn3-F7: $1.942(10)$ | F4-F7: $2 \times 2.721$ | 84.2(3) |
| Zn3-F6: $1.951(12)$ | F3-F4: $2 \times 2.742$ | 83.3(3) |
| Zn3-F3 ${ }^{\text {b }}$ : $2 \times 2.004(6)$ | F4-F6: $2 \times 2.814$ | 87.0 (3) |
| Zn3-F4 ${ }^{\text {b }}$ : $2 \times 2.127(7)$ | F3-F6: $2 \times 2.884$ | 93.2 (3) |
|  | F3-F7: $2 \times 2.902$ | 94.4 (3) |
|  | F4-F4 2.978 | 89.1(4) |
| F6-Ln3-F7: 167.7(4) | F3-F3: $\quad 3.158$ | 104.0(3) |
| Zn4 octahedron: Symmetry 2 |  |  |
| Zn4-F5 ${ }^{\text {b }}$ : $2 \times 1.996(6)$ | F8-F8: 2.651 | 82.0(4) |
| Zn4 F8b: $2 \times 2.016$ (7) | F5-F5: $\quad 2.721$ | 86.3(4) |
| Zn4-F3 ${ }^{\text {b }}$ : $2 \times 2.032(7)$ | F3-F5: $2 \times 2.799$ | 88.0(3) |
| (Zn4-F) 2.014 | F3-F5: $2 \times 2.832$ | 89.3(3) |
| Zn4-F5-Zn4: 93.7(4) | F3-F8: $2 \times 2.902$ |  |
| Zn4-F8-Zn4: 92.54) | F3-F8: $2 \times 2.903$ | 91.3(3) |
| F3-Zn4-F3: 176.84) | F5-F8: $2 \times 2.978$ | $95.8(3)$ |
| Zn4-Zn4: 2.913(3) |  |  |
| (Zn-F') $1.980\left\langle\mathrm{Zn}-\mathrm{F}^{\text {b }}\right\rangle \mathbf{2 . 0 4 0}$ |  |  |
| (Zn-F) 2.025 |  |  |

TABLE V
Coordination of Fluorine Ions with the Different $\mathbf{Z n}^{2+}$ in the Structure

|  |  | Distance (Ä) |
| :---: | :---: | :---: |
| Onefold | Terminal |  |
|  | $\mathrm{FI} \rightarrow \mathrm{Zn} 2$ | 1.994 |
|  | $\mathrm{F} 2 \rightarrow \mathrm{Zn} 2$ | 2.001 |
|  | F6 $\rightarrow \mathrm{Zn} 3$ | 1.951 |
|  | $\mathrm{F} 7 \rightarrow \mathrm{Zn} 3$ | 1.942 |
|  | $\left\langle\mathrm{Zn}-\mathrm{F}^{\prime}\right\rangle=1.980(30)$ |  |
| Twofold | Bridging (b2) |  |
|  | $\mathrm{F} 3 \rightarrow\left\{\begin{array}{l} \mathrm{Zn} 3 \\ \mathrm{Zn} 4 \end{array}\right.$ | 2.004 |
|  |  | 2.032 |
|  | $\mathrm{F4} \rightarrow\left\{\begin{array}{l}\mathrm{Zn} 1 \\ \mathrm{Zn} 3\end{array}\right.$ | 2.025 |
|  |  | 2.127 |
|  | F5 $\rightarrow\left\{\begin{array}{l}\mathrm{Zn} 4 \\ \mathrm{Zn} 4\end{array}\right.$ | 1.996 |
|  |  | 1.996 |
|  | F9 $\rightarrow\left\{\begin{array}{l}\mathrm{Zn} 1 \\ \mathrm{Zn} 2\end{array}\right.$ | 1.943 |
|  |  | 2.276 |
|  | $\left\langle 7 . \mathrm{n}-\mathrm{F}^{62}\right)=2.050(105)$ |  |
| Threefold | Bridging (b3) |  |
|  | Zn2 | 2.031 |
|  | $\mathrm{FB} \rightarrow\{\mathrm{Zn4}$ | 2.016 |
|  | Zn4 | 2.016 |
|  |  | 2.021(9) |
|  |  | $2.035(20)$ |

TABLE VI
Valence Bond Analysis of $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ Using the Zachariasen Law ${ }^{a}$

|  | Znl | Zn 2 | Zn3 | Zn4 | Bal | Ba 2 | Ba3 | $\Sigma$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F1 ${ }^{1}$ | - | $2 \times 0.380$ | - | - | $2 \times 0.230$ | $2 \times 0.181$ | - | 1.105 |
|  |  |  |  |  |  | $2 \times 0.314$ |  |  |
| F2 ${ }^{\text {²}}$ | - | $2 \times 0.320$ | - | - | $2 \times 0.270$ | - | $2 \times 0.193$ | 1.107 |
|  |  |  |  |  |  |  | $2 \times 0.274$ |  |
| F3 ${ }^{\text {b2b }}$ | - | - | $2 \times 0.366$ | $2 \times 0.329$ | - | $2 \times 0.167$ | $2 \times 0.196$ | 1.058 |
| F4 ${ }^{62}$ | $4 \times 0.398$ | - | $2 \times 0.228$ |  | $2 \times 0.168$ | $2 \times 0.040$ | $2 \times 0.075$ | 0.918 |
|  |  |  |  |  | $2 \times 0.069$ |  |  |  |
| F5 ${ }^{\text {b2 }}$ | - | - | - | $2 \times 0.377$ | - | 0.136 | 0.067 | 0.957 |
| F6 ${ }^{\text {t }}$ | - | - | 0.449 | - | 0.319 | $2 \times 0.095$ | - | 0.958 |
| F71 | - | 一 | 0.465 | - | 0.204 | - | 0.089 | 0.966 |
|  |  |  |  |  |  |  | $2 \times 0.104$ |  |
| F8 ${ }^{\text {b3b }}$ | - | 0.330 | - | $2 \times 0.349$ | - | - | - | 1.028 |
| F9 ${ }^{\text {b2b }}$ | $2 \times 0.397$ | 0.128 | - | - | $2 \times 0.111$ | $2 \times 0.156$ | - | 1.059 |
| $\Sigma$ | 2.014(8) | $1.9615)$ | 2.10(7) | 2.11(5) | 2.22(4) | 1.89 (3) | 1.84(3) | - |
| $\Sigma_{\text {theor }}$ | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |

[^0]and the corresponding distances are in good agreement with previous data ( 10,11 ) and the sum of ionic radii (12). However, the situation of the $\mathrm{Zn} 2-\mathrm{F} 9$ bond ( $2.276 \AA$ ) seems anomalous. A valence bond analysis ( 9,14 ), which appears in Table VI, shows that the bond strength of F9 is approximately three times lower than the others around Zn 2 and explains that a long $\mathrm{Zn} 2-\mathrm{F} 9$ distance is normal, the bonding possibilities of Zn 2 being quite "saturated" by the fluorine F1, F2, and F8. The coordination of Zn 2 is then better described by $(5+1)$ than 6 . This fact is correlated to the short F1-F2 distances. $\mathrm{Zn}^{2+}$ cannot be inserted in the square plane of $F 1$ and $F 2$ ions (the permitted radius is only $0.67 \AA$ compared to $r_{\mathrm{Zn}} 2+$ $=0.74 \AA$ ). It shifts out of the plane; the presence of Ba 1 and Ba 2 ions near F 9 and F1 obliges $\mathbf{Z n}^{2+}$, for electrostatic repulsion reasons, to be displaced toward F8. The $\mathrm{Zn} 2-\mathrm{F} 9$ distance is then increased.

The $\mathrm{ZnF}_{6}$ octahedra share edges and corners to ensure a three-dimensional network. In the ( 002 ) plane, octahedra of Zn 4 ions (shaded in Fig. 1) form infinite rutile
chains parallel to the $\mathbf{b}$ axis of the cell, the dimension of which corresponds to two edge-sharing octahedra. Zn 2 and Zn 3 octahedra share some of their corners with Zn 1 and Zn 4 octahedra in a rather complicated way. Two different types of description render the analysis of their connection easier: the first uses connected layers, the second starts from defective rutile blocks. In each case, it will be necessary to compare the networks of $\mathrm{Ba}_{6} M_{7} \mathrm{~F}_{26}(M / \mathrm{Ba}=1.167)$ and $\mathrm{Ba}_{2} M_{3} \mathrm{~F}_{10}(M / \mathrm{Ba}=1.50)$. Then, a possible mechanism of structural evolution in the $M / \mathrm{Ba} \geq 1$ part of the binary diagram $\mathrm{BaF}_{2}-M \mathrm{~F}_{2}$ will be proposed, the limit of this evolution being the rutile structure.

## 1. Connected Layers

The connection of $\mathrm{Zn} 1, \mathrm{Zn} 3$, and Zn 4 octahedra in the (200) plane builds layers which appear in Fig. 2a. In these layers, two consecutive rutile chains ( Zn 4 octahedra) are separated by a complete planar perovskite block, i.e., three rows ( $\mathrm{Zn} 3-$ $\mathrm{Zn} 1-\mathrm{Zn} 3$ ) of corner-sharing octahedra. Two consecutive layers are shifted of $b / 2$


Fig. 2. (a) Perspective view of the layer in the (200) plane. Full circles indicate the fluorine atoms shared with the Zn 2 isolated octahedra which ensure the connection between two layers. For this symbolism, there is no correlation with those of Fig. I. (b) Proposed intermediate step for the transformation from $\mathrm{Ba}_{6} \mathrm{M}_{7} \mathrm{~F}_{26}$ to $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$. (c) Perspective view of the layer in the (002) plane of the $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ structure. (d) Extrapolated intermediate step in the condensation of $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$. (e) Perspective view of the layer of a possible structure corresponding to $\mathrm{Ba}_{2} \mathrm{M}_{5} \mathrm{~F}_{14}$ formulation.
and linked by isolated Zn 2 octahedra. This last octahedron shares the F8 ion with the rutile chain of one layer, and F9 with the medium row Zn 1 of the perovskite block of the other layer (owing to the $b / 2$ shift mentioned above). These layers correspond to the main faces of the platelet.

A similar situation exists in the previously described (5) $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ (Fig. 2c), but only two rows of corner-sharing octahedra separate two rutile chains. This corresponds to the elimination of one Zn 3 row in the $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ structure and to a correlated shift of the rutile chain according to the
scheme of Fig. 2b. This figure also explains the change of the nature of the layer bridging units. They were single Zn 2 octahedra in $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ and became isolated bioctahedra in $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$. Such a procedure corresponds to a condensation mechanism. If it is extrapolated, (Fig. 2d), it may be assumed that the following step, unknown in the diagram at the present time, would lead to the structure which appears in Fig. 2e. The corresponding formula would be $\mathrm{Ba}_{2} \mathrm{M}_{5} \mathrm{~F}_{14}$. In this hypothesis, it is noteworthy that the bridging isolated bioctahedra would be connected to each other in order


Fig. 3. (a) Perspective view of the deficient rutile blocks in $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$. Zn vacancies are noted by open squares and $\mathrm{Ba}^{2+}$ ions by open circles. (b) Perspective view of the corresponding rutile structure.
to form planes identical to those which exist in the $\mathrm{CaTa}_{2} \mathrm{O}_{6}$ structure (13). However, the interstices occupied by $\mathrm{Ba}^{2+}$ ions would be relatively small; in other words, if such a structure does exist, it can only be with smaller alkaii earth ions.

## 2. Defective Rutile Blocks

From Fig. 1, it can be seen that each Zn4 chain is surrounded by four satellite octahedra ( $2 \mathrm{Zn} 2+2 \mathrm{Zn} 3$ ). Their projection on the (010) plane is reminiscent of the rutile structure. However, the perspective views of Fig. 3 illustrate the difference between these two units. In the rutile structure (Fig. 3b), the satellites form also chains of edgesharing octahedra, whereas in $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ (Fig. 3a), half of the $3 d$ metallic sites are missing. Satellite chains of the rutile structure become a succession of filled octahedra separated by $\mathrm{Ba}^{2+}$ ions which roughly occupy the corresponding $\mathrm{F}^{-}$sites in the rutile structure. In $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$, Znl octahedra ensure the connection of these blocks (Fig. 4a). In $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$, identical units are directly connected one to the other (Fig. 4 b ), owing to the condensation mechanism proposed above. The further progressive transformation into the rutile structure would occur by the replacement of $\mathrm{Ba}^{2+}$ by $3 d M^{2+}$ ions, simultaneously with the change of terminal $\mathrm{F}^{-}$into bridging ones.

The coordination polyhedra of $\mathrm{Ba} 1, \mathrm{Ba} 2$, and Ba3 can be easily described if the (201) planes of the structure are considered: barium and fluorine ions form together slightly distorted dense packing layers parallel to these planes; barium ions adopt the 12-coordination characteristic of this type of packing. In the pseudo-orthorhombic cell (Fig. 5) obtained by the matrix

$$
\left[\begin{array}{l}
a_{0} \\
b_{0} \\
c_{0}
\end{array}\right]=\left[\begin{array}{lll}
2 & 0 & \overline{1} \\
0 & 1 & 0 \\
1 & 0 & 2
\end{array}\right]\left[\begin{array}{l}
a_{\mathrm{m}} \\
b_{\mathrm{m}} \\
c_{\mathrm{m}}
\end{array}\right],
$$

the structure can be described in terms of dense packing with 12 layers corresponding to the sequence $A_{4}^{1,2} B_{2}^{3} A_{2}^{3} B_{4}^{1,2} C_{4}^{1,2} A_{2}^{3} C_{2}^{3} A_{4}^{1,2}$


Fig. 4. Relative disposition of the defective rutile blocks in $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ (a) and $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ (b) projections on the ( 010 ) plane. The representation of rutile and perovskite blocks appears between (a) and (b).


Fig．5．Representation of $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}$ in terms of dense packing（the first 20 layers have been repre－ sented）．The symbols for $\mathrm{Ba}^{2+}$ ions are the same as that in Fig． 1.
$B_{4}^{1,2} C_{2}^{3} B_{2}^{3} C_{4}^{1,2}$ ．In this notation，the higher in－ dices refer to the type of $\mathrm{Ba}(\mathrm{Ba} 1, \mathrm{Ba} 2$ ，or Ba 3 ）which is inserted in the considered layer，and the lower ones（ 2 or 4 ）to the number of barium ions in the layer．These indices correspond to the compositions $\mathrm{Ba}_{2} \mathrm{~F}_{14}$ for indice 2 and $\mathrm{Ba}_{4} \mathrm{~F}_{12}$ for indice 4 which were encountered also in $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ ， but with a different mode of stacking．Con－ sequently，the three（4i）sites of $\mathrm{Ba}^{2+}$ adopt a 12－coordination of the hcp type for Ba3 and of the fcc type for both Ba 1 and Ba 2 ． Keeping in mind that in rutile，the close packing of $\mathrm{F}^{-}$is exclusively of the hcp type，it is normal to ascertain the increase of the percentage of this type of site $\mathbf{( 3 3 . 3 \%}$ in $\mathrm{Ba}_{6} \mathrm{Zn}_{7} \mathrm{~F}_{26}, 50 \%$ in $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}, 100 \%$ in $M \mathrm{~F}_{2}$ ）with the $M / \mathrm{Ba}$ ratio．

In all the cases（Table VII），the average value of $\mathrm{Ba}-\mathrm{F}$ distances（ $2.848 \AA$ for Ba ， $2.937 \AA$ for $\mathrm{Ba} 2,2.920$ Å for $\mathrm{Ba} 3,\langle\mathrm{Ba}-\mathrm{F}\rangle=$ $2.901 \AA$ ）is very close to the sum of ionic radii of ${ }^{\mathrm{XI}} \mathrm{Ba}^{2+}(1.61 \AA)$ and ${ }^{11} \mathrm{~F}^{-}(1.285 \AA)$ （12）． $\mathrm{F}-\mathrm{F}$ distances being always longer than $2 r_{\mathrm{F}^{-}}$，it can be thought that the inser－ tion of $\mathrm{Ba}^{2+}$ ions in the fluorine layers is responsible of this observed increase of dis－ tance between $\mathrm{F}^{-}$ions，and consequently of the decrease of the packing ratio $\tau$ from 0.74 ideal value to 0.608 when only $\mathrm{Ba}^{2+}$

TABLE VII
Interatomic Distances（ $\AA$ ）in the Coordination Polyhedra of $\mathrm{Ba}^{2+}$

Polyhedra of Bal
Bal－F6：2．589（12）
Ba1－F2： $2 \times 2.655(6)$
Bal－FI： $2 \times 2.718(6)$
Bal－F7：$\quad 2.765(4)$
Bal－F4： $2 \times 2.841(10)$
Ba1－F9： $2 \times 3.004(2)$
Ba1－F4： $2 \times 3.194(11)$
（Ba1－F〉 2.848
Polyhedra of Ba 2
Ba2－FI： $2 \times 2.595(6)$
$\mathrm{Ba} 2-\mathrm{Fl}: 2 \times 2.811(6)$
Ba2－F3： $2 \times 2.843(7)$
Ba2－F9：$\quad 2.870(12)$
Ba2－F5：2．924（9）
Ba2－F6： $2 \times 3.066(3)$
Ba2－F4： $2 \times 3.412(10)$
（Ba2－F） 2.937
Polyhedra of Ba 3
Ba3－F2： $2 \times 2.649$（6）
Ba3－F3： $2 \times 2.781(7)$
Ba3－F2： $2 \times 2.786(7)$
Ba3－F7： $2 \times 3.030(2)$
Ba3－F7： 3.090 （2）
Ba3－F4： $2 \times 3.160(12)$
Ba3－F5：3．201（9）
（Ba3－F） 2.920
〈Ba－F〉 2.901
and $\mathrm{F}^{-}$are considered（ $\tau=0.63$ when $\mathrm{Zn}^{2+}$ are included）．

## Conclusion

This study，and the previously described $\mathrm{Ba}_{2} \mathrm{Ni}_{3} \mathrm{~F}_{10}$ structure have begun to show that，in the binary diagrams $(1-x) \mathrm{BaF}_{2}$ ， $x M \mathrm{~F}_{2}$ ，the structural evolution in the $x>$ 0.5 region may be described by a condensa－ tion mechanism for $0.714 \geq x>0.5$ ．It could explain the transformation of struc－ tures deriving from the perovskite to the rutile structure．At the present time，the validity of the mechanism is studied for
higher values of $x$, particularly in $\mathrm{Ba}_{2} \mathrm{Cu}_{7} \mathrm{~F}_{18}$ single crystals.

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[^0]:    ${ }^{a} S=\exp \left(D_{0}-D\right) / B . D_{0}$ represents the length of a bond in a regular polyhedron and $B$ a fitted constant: $D_{0}=2.028(2)$ and $B=0.2598$ for $\mathrm{Zn}-\mathrm{F} ; D_{0}=2.685(2)$ and $B=0.394$ for $\mathrm{Ba}-\mathrm{F}$. ${ }^{b} b 2$ and $b 3$ refer to the two types of bridging fluorine (see Table V).

